



## Lognormal Upper Tail of Rainfall Intensity and POT Values: Implications on the IDF Curves

C. Lepore (1,2), D. Veneziano (3) and A. Langousis (3)

(1) Dipartimento di Ingegneria Civile, Università degli Studi di Salerno, Fisciano, Italy (clepore@unisa.it), (2) Instituto do Mar-Centro Interdisciplinar de Coimbra, Portugal, (3) Department of Civil and Environmental Engineering, MIT, Cambridge, U.S.A.

Let  $I(d)$  be the average rainfall intensity in an interval of duration  $d$  and denote by  $I(d; i^*)$  the peak-over-threshold (POT) value of  $I(d)$  for threshold  $i^*$  and by  $I_{max}(d)$  the annual maximum of  $I(d)$ .

Hydrologic risk assessment and design depend critically on the upper tail of the distribution of  $I_{max}(d)$ . Since the events  $I(d) > i$  in non-overlapping  $d$ -intervals become independent as  $i$  becomes large and for even moderate thresholds  $i^*$  the excursions of  $I(d)$  above  $i^*$  may be considered Poisson, the upper tail of the distribution of  $I_{max}(d)$  may be estimated from the upper tails of  $I(d)$  and  $I(d; i^*)$  as

$$P[I_{max}(d) > i] \approx \{P[I(d) > i/\gamma]\}^{1/d} \quad (1)$$

$$P[I_{max}(d) > i] \approx e^{-\lambda_{i^*} P[I(d; i^*) > i - i^*]} \quad (2)$$

where  $d$  is in years,  $\gamma$  is a continuity correction factor around 1.15, and  $\lambda_{i^*}$  is the average annual exceedance rate of threshold  $i^*$ . Based on (1), it has been argued that the distribution of  $I_{max}(d)$  should be of the GEV type, with recent propensity for EV2. This is consistent with results from (2) if  $I(d; i^*)$  has GP distribution. However, the GEV claim follows from (1) under asymptotic conditions that may not be attained for the upper tail of  $I_{max}(d)$  and from (2) under the assumption that  $I(d; i^*)$  is GP-distributed, which may not hold.

We take another look at the distributions of  $I(d)$  and  $I(d; i^*)$  and their implications on the upper tail of  $I_{max}(d)$  through (1) and (2). Specifically we show that there is

empirical and theoretical evidence that for durations  $d \leq 1$  day the upper tail of  $I(d)$  has a lognormal behavior over a wide range of intensities and that also the distribution of  $I(d; i^*)$  has a significant lognormal range. These conclusions are supported by both historical and simulated rainfall records and theoretical analysis. For the simulations we use a partly theoretical model in which storm occurrence times and durations are extracted from a historical record but the storm intensity and within-storm fluctuations are generated randomly, the latter using a beta-lognormal multifractal process.

Results on  $I_{max}(d)$  obtained from (1) and (2) by fitting distributions of  $I(d)$  and  $I(d; i^*)$  with upper lognormal tails are compared to results from directly fitting a GEV distribution to the observed annual maximum intensities and from using (2) with a fitted GP distribution of  $I(d; i^*)$ .

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