



## **Predicting regional hydrological response to climate change using a water-energy coupled balance model based on the Budyko and Bouchet hypotheses**

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Areal evaporation ( $E$ ) on the long time scale is primarily controlled by the available energy and water. Thereinto the available energy can be measured by potential evaporation ( $E_0$ ), and the available water can be represented by precipitation ( $P$ ). In other words,  $E$  can be expressed as a function of  $E_0$  and  $P$ . The function is called water-energy balance equation, which can be expressed as  $E = E_0 P / (P^n + E_0^n)^{1/n}$ , with  $n$  being a parameter representing the catchment characteristics. Due to the feedback of atmosphere on land surface,  $E$  increases as a result of increasing  $P$ ; and it will lead to a decrease in  $E_0$  according to the complementary relationship between actual and potential evaporation. If we express  $P$ ,  $E_0$  and  $E$  as a point ( $P$ ,  $E_0$ ,  $E$ ) in the state space, as a result of precipitation changing from  $P_1$  to  $P_2$ , the state changes from an initial state ( $P_1$ ,  $E_{0,1}$ ,  $E_1$ ) to a new state, not being ( $P_2$ ,  $E_{0,1}$ ,  $E_2$ ), but ( $P_2$ ,  $E_{0,2}$ ,  $E_2$ ). In other words, the water-energy balance equation cannot evaluate the change in  $E$  because of  $E_0$  having a change. To calculate ( $P_2$ ,  $E_{0,2}$ ,  $E_2$ ), another function is introduced from the complementary relationship (CR) between potential and actual evapotranspiration as  $bE + E_0 = (1+b) E_w$ , where  $b$  is a constant of proportionality;  $E_w$  is the wet environment evapotranspiration, which can be calculated from the net radiation ( $R_n$ ) by the Priestley-Taylor equation. It can be notable that these two equations have two independent variables ( $P$  and  $R_n$ , not being interrelated, i.e.  $\partial P / \partial R_n = 0$ ), therefore the two dependent variables ( $E$  and  $E_0$ ) can be resolved. This implies that a relatively stable state ( $P$ ,  $E_0$ ,  $E$ ) can be reached

in a given catchment under particular radiation and precipitation. Simultaneously, equations  $dE = \partial E / \partial P \cdot dP + \partial E / \partial E_0 \cdot dE_0$  (derived from the water-energy balance equation) and  $bdE + dE_0 = (1+b) dE_w$  (derived from the CR) lead to the expression  $dE = [\partial E / \partial P \cdot dP + (1 + b) \partial E / \partial E_0 \cdot dE_w] / (1 + b \partial E / \partial E_0)$ . The regional response of the hydrologic cycle ( $dE$  and  $dR = dP - dE$ ) to climate changes  $dE_w$  ( $dT$  and  $dR_n$ ) and  $dP$  can be predicted.