



Continuous time random walk description of non-Fickian transport

B. Berkowitz and H. Scher

Department of Environmental Sciences and Energy Research, Weizmann Institute of Science, Rehoto 76100 Israel

The continuous time random walk (CTRW) framework offers an effective means to quantitatively describe non-Fickian transport in a wide variety of porous and fractured geological formations. The source of non-Fickian behavior is due to the broad spectrum of transition rates that control solute movement. Two principal mechanisms can generate such a spectrum: flow in the complex velocity field of a disordered medium and mass exchange between a mobile phase and a distribution of immobile states. Both of these mechanisms are incorporated into the CTRW framework, which is based on a picture of transport as a sequence of particle transition rates (e.g., between pore spaces, fracture intersections) with displacements s and times t , and the incorporation of the full spectrum of these rates into the transport equations. But even in small-scale, “homogeneous” porous media, subtle and residual pore-scale disorder effects can lead to non-Fickian transport. A central focus of the CTRW approach is an accurate physical model of the entire spectrum $\psi(s, t)$. We find that the uncoupled form, $p(s)\psi(t)$, is an effective representation in many practical situations, although we identify some specific cases where coupled forms of $\psi(s, t)$ are required. We consider solute interaction dynamics as a function of the spectra of advective-diffusive transition times and exchange times, and the relative separation of their respective time domains. We first examine a physical situation in which these two different types of spectra are distinguishable, so that a more complete characterization of the transport can be obtained (i.e., rather than lumping all the rates together). Experimental data are analyzed from a sorbing species transported through a heterogeneous porous domain, and the CTRW is shown to produce excellent fits and predictions, using a single set of param-

eters. We then focus on observations of non-Fickian transport in two series of sandbox experiments. We represent the main features of the transport in terms of a truncated power-law (TPL), $\psi(t) \sim (t_1 + t)^{-1-\beta} \exp(-t/t_2)$, where t_1 and t_2 are the limits of the power-law spectrum. An excellent fit to the entire BTC data set (including the changes in flow velocity) for each sandbox medium is accomplished with a single set of values of t_1, β, t_2 . The use of the full spectrum of $\psi(t)$ is necessary to describe the transition to Fickian behavior, and to account for the dynamics of non-Fickian transport.