



Turbulent viscosity and lifetime of Saturn's rings

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The viscosity (the angular momentum flux) in the disk of mutually gravitating particles of Saturn's rings is investigated. The hydrodynamic theory of the gravitational Jeans-type instability of small gravity perturbations (e.g., those produced by spontaneous disturbances) of the disk is developed. It is suggested that in such a system the self-sustained hydrodynamic turbulence may arise as a result of the instability. The turbulence is related to stochastic motions of "fluid" elements. The objective of this paper is to show that in the Jeans-unstable Saturnian ring disk the turbulent viscosity may exceed the ordinary microscopic viscosity substantially. The main result of local N -body simulations of planetary rings by Daisaka et al. (2001, *Icarus* **154**, 296-312) is explained: in the presence of the gravitationally unstable density waves, the effective turbulent viscosity ν_{eff} is given as $\nu_{\text{eff}} = CG^2\Sigma^2/\Omega^3$, where G , Σ , and Ω are the gravitational constant, the surface mass density of a ring, and the angular velocity, respectively, and the non-dimensional correction factor $C \approx 10$. We argue that both Saturn's rings and their irregular of the order of 100 m or even less fine-scale structure are not likely much younger than the solar system.