



Lévy flights: transitions and meta-stability

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We consider a dynamical system $dX_t^\varepsilon = -U'(X_t^\varepsilon)dt + \varepsilon dL_t$ which can be seen as a deterministic system $dX_t^0 = -U'(X_t^0)dt$ perturbed by symmetric stable Lévy noise (Lévy flights) L of small intensity.

Using probabilistic argument, we determine the exit law of X^ε from intervals containing a unique asymptotically stable attractor of X^0 . In the case of the double-well potential U , we study the asymptotics of the transitions times and metastable behaviour of the jump diffusion.

Due to the heavy-tail nature of the process L , our results differ strongly from the well known case of Gaussian perturbations (Freidlin–Wentzell theory).

Our research is motivated by works by P. Ditlevsen who observed stable noises in Greenland ice-core data.