



## Using magnetic liquids to simulate convection in a radial force field

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Convection in a radial force field is a central problem of convection in planetary interiors, including the Earth's core and mantle. Common laboratory experiments, however, only allow the investigation of convection in a unidirectional and constant gravity field.

Magnetic liquids are manufactured suspensions of magnetic nanoparticles in a carrier liquid of suitable choice. The particles possess a fixed magnetic moment and are coated with a surfactant to prevent coagulation. When an external magnetic field is applied, the resulting orientation of the particles results in a net magnetisation of the fluid which depends both on the applied field and the temperature of the fluid. The fluid then experiences a body force towards stronger magnetic fields, known as the Kelvin force,  $f = \mu_0 M |\nabla H|$ . A local variation in temperature will result in a local variation of the Kelvin force, resulting in a magnetic equivalent to natural convection.

The equivalence between natural convection and thermomagnetic convection can be quantified by equating the volume expansion coefficient,  $\alpha_0$ , with the temperature sensitivity of the magnetisation,  $(\partial M / \partial T)_H$ , known as the pyromagnetic coefficient, and the gravity potential with the magnetic field,  $H$  (or gravity,  $g$ , with the field gradient,  $|\nabla H|$ ). This leads to a thermomagnetic Rayleigh number as defined by

$$Ra_m = \frac{L^3}{\nu \kappa} \frac{\mu_0}{\rho} \left( \frac{\partial M}{\partial T} \right)_H |\nabla H| \Delta T, \quad (1)$$

compared to the standard Rayleigh number as

$$Ra = \frac{L^3}{\nu \kappa} \alpha_0 g \Delta T,$$

where  $L$  is the length scale,  $\mu_0 = 4\pi \times 10^{-7}$  the permeability of free space.  $\nu$  and  $\kappa$  are the kinematic viscosity and thermal diffusivity, respectively.

Using fairly standard magnets and magnetic liquids, the pyromagnetic coefficient is  $O(10\text{Am}^{-1}\text{K}^{-1})$ , and field gradients can be  $O(10^4 - 10^7\text{Am}^{-2})$ . This can lead to magnetic Rayleigh numbers of the same order as  $Ra$ , or even some orders of magnitude larger than the standard Rayleigh number.

In this paper, we will present a relatively simple, 2D finite-element model of a proposed laboratory experiment to use a magnetic liquid in a spherical shell, where a permanent magnet is embedded in the inner core of the experiment. This will be compared with an equivalent model assuming a central gravity field. The comparison between these two experiments will be put into the context of an existing experiment of natural and magnetic Rayleigh-Bénard convection of a magnetic liquid in a box. This experiment, and a corresponding finite-element model, have shown that convection could be initiated by the presence of a magnet on top, or to the side of the box despite a stabilising temperature gradient (i.e. cooled from below). Conversely, a magnet positioned below the box could inhibited natural convection effectively if the box was heated from below.