



Short and long memory unobserved components in hydrological time series

M. Corduas

Dipartimento di Scienze Statistiche, Università di Napoli Federico II, Via L. Rodinò 22, 80138 Naples -I (corduas@unina.it /Fax: +39 081 2537466)

In this work we discuss the problem of estimating unobserved components in short and long memory hydrological time series. In particular, we focus our attention on *Decomel* (Piccolo, 1979, 1982). This is a statistical method to decompose a stochastic process $Z_t \sim ARMA(p, q)$ into the sum of two independent processes $X_t \sim ARMA(p_x, q_x)$ and $Y_t \sim ARMA(p_y, q_y)$. The method relies on four main steps:

- i) to identify the conditions for the decomposition and the orders $(p_x, q_x; p_y, q_y)$;
- ii) to search for the parameter vector $\beta = (\beta_x, \beta_y)'$ characterizing the *AR* and *MA* operators of the component processes such that:

$$G(\beta) = \int_{-\pi}^{\pi} (f_z(\omega) - f_x(\omega; \beta_x) - f_y(\omega; \beta_y))^2 d\omega = \min!$$

where $f_z(\omega)$, $f_x(\omega; \beta_x)$, $f_y(\omega; \beta_y)$ are the spectra of the Z_t , X_t , Y_t , respectively;

- iii) to check for the admissibility conditions, that is, the strict positiveness of the estimated spectra of the components;
- iv) to evaluate the filter weights needed to extract the components from the series by standard Wiener-Kolmogorov theory.

The integral is computed over a grid of discrete points. This results in a non-linear regression problem.

In this article we discuss how the procedure can be fruitfully applied to analyse hydrological time series. Firstly, we modify *Decomel* to make it a semiparametric method.

Secondly, we discuss an extension of the decomposition procedure to long memory time series. An application to some river flow time series conclude the work.

Essential References

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